

**24th Benelux Meeting**  
**on**  
**Systems and Control**

**March 22 – 24, 2005**

**Houffalize, Belgium**

**Book of Abstracts**

**Laurent Catoire, Michel Kinnaert and Alain Vande Wouwer**  
**Book of Abstracts 24th Benelux Meeting on Systems and Control**

Université Libre de Bruxelles - Dept. of Control Engineering and System Analysis  
CP165/55, 50 av. F.D. Roosevelt B-1050 Brussels Belgium

Faculté Polytechnique de Mons - Service d'Automatique  
31 boulevard Dolez B-7000 Mons Belgium

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**WEP05-3** **18.05–18.30**  
*The Zeno phenomenon in the triple integrator with relay feedback* ..... 124  
 J.M. Schumacher Tilburg University

**WEP06** **Vellereux**  
**Automotive systems II**  
**Chair: Erik Noldus** **17.15–18.30**

**WEP06-1** **17.15–17.40**  
*Measurement and Control of slip in a CVT* ..... 125  
 Bram Bonsen Eindhoven University of Technology  
 M Steinbuch  
 PA Veenhuizen

**WEP06-2** **17.40–18.05**  
*Decoupling feedback control applied on a half-car test rig* ..... 126  
 D. Vaes K.U.Leuven  
 K. Smolders K.U.Leuven  
 J. Swevers K.U.Leuven

**WEP06-3** **18.05–18.30**  
*The establishment and analysis on the inverse model of the vehicle transmission systems* ..... 127  
 Pan Hongxia University Hannover  
 Yao Zhuting North University of China

**Thursday, March 24, 2005**

**Mini Course: P5** **Vissoule**  
**An introduction to optimum experimental design**  
**Professor Luc Pronzato (France)**  
**Chair: Michel Kinnaert** **8.30– 9.30**

*An introduction to optimum experimental design and related control problems (lecture 2)* ..... 213  
 Professor Luc Pronzato (France)

**Plenary: P6** **Vissoule**  
**Dynamics and Control of Microchemical Systems**  
**Professor Mayuresh V. Kothare (USA)**  
**Chair: Alain Vande Wouwer** **9.40–10.40**

*Dynamics and Control of Microchemical Systems* ..... 306  
 Professor Mayuresh V. Kothare (USA)

**Mini Course: P7** **Vissoule**  
**An introduction to optimum experimental design**  
**Professor Luc Pronzato (France)**  
**Chair: Christine Renotte** **11.10–12.10**

*An introduction to optimum experimental design and related control problems (lecture 3)* ..... 213  
 Professor Luc Pronzato (France)

**THP01** **Vissoule**  
**Model reduction**  
**Chair: Peter Heuberger** **13.40–15.20**

**THP01-1** **13.40–14.05**  
*L<sub>2</sub>-approximation of wavelet functions* ..... 128

J.M.H. Karel Universiteit Maastricht  
 R.L.M. Peeters Universiteit Maastricht  
 R.L. Westra Universiteit Maastricht  
 S.A.P. Haddad, W.A. Serdijn

**THP01-2** **14.05–14.30**  
*Image transformation and compression using realization theory and balanced model reduction* ..... 129  
 Bart Vanluyten KULeuven  
 Bart De Moor KULeuven

**THP01-3** **14.30–14.55**  
*Model Reduction of Interconnected Systems* ..... 130  
 Antoine Vandendorpe Université catholique de Louvain  
 Paul Van Dooren Université catholique de Louvain

**THP01-4** **14.55–15.20**  
*Control-Oriented Identification of the Impact CVT* . . . . 131  
 Tim Klaassen Eindhoven University of Technology

**THP02** **Wandebourcy**  
**Control of chemical processes**  
**Chair: Christine Renotte** **13.40–15.20**

**THP02-1** **13.40–14.05**  
*Development of a chemical plant hybrid automaton model for on-line scheduling optimization* ..... 132  
 Iliyana Simeonova Université Catholique de Louvain  
 Georges Bastin Université Catholique de Louvain  
 Denis Dochain Université Catholique de Louvain

**THP02-2** **14.05–14.30**  
*Controllability analysis of industrial crystallizers* . . . . 133  
 A.N. Kalbasenka Delft University of Technology

**THP02-3** **14.30–14.55**  
*Contribution to the control of a rotary cement kiln - A simulation* ..... 134  
 A.C. Witsel Faculté Polytechnique de Mons  
 C. Renotte Faculté Polytechnique de Mons  
 M.Remy Faculté Polytechnique de Mons

**THP02-4** **14.55–15.20**  
*Optimal control of a batch reactor under model uncertainty* ..... 135  
 Renato Lepore Faculté Polytechnique de Mons  
 Dr Prof. Alain Vande Wouwer Faculté Polytechnique de Mons  
 Dr Prof. Marcel Remy Faculté Polytechnique de Mons  
 R. Findeisen, Z. Nagy, F. Allgöwer

**THP03** **Rensiwez**  
**Mechanical systems III**  
**Chair: Georges Bastin** **13.40–15.20**

**THP03-1** **13.40–14.05**  
*Active control for an inkjet printhead* ..... 136  
 M.B. Groot Wassink Delft University of Technology  
 Sjirk Koekebakker Océ-Technologies B.V.

**THP03-2** **14.05–14.30**  
*Improving performance of inkjet printing systems by means of low-cost mechatronics* ..... 137  
 Dennis Bruijnen Technische Universiteit Eindhoven

# L<sub>2</sub>-Approximation of Wavelet Functions

Joël Karel, Ralf Peeters and Ronald Westra

Department of Mathematics, Universiteit Maastricht

P.O. Box 616, 6200 MD Maastricht, The Netherlands

joel.karel@math.unimaas.nl, ralf.peeters@math.unimaas.nl, westra@math.unimaas.nl

Sandro Haddad and Wouter Serdijn

Electronics Research Laboratory, Faculty of Information Technology and Systems, TU Delft

Mekelweg 4, 2628 CD Delft, The Netherlands

s.haddad@its.tudelft.nl, w.a.serdijn@its.tudelft.nl

## 1 Introduction

Computations in the analog domain are significantly less power consuming than computations in the digital domain, mainly due to the power consumption of A/D-converters. It is therefore opportunistic to perform computations in the analog domain for applications where power consumption is a critical issue. Wavelet transformations  $W(t, \sigma)$  can be performed in the analog domain by approximating them with linear systems (LS). In earlier work [1] this was accomplished with Padé-approximation of wavelet functions for implementation in dynamic translinear (DTL) circuits that are current- instead of voltage-based which offers a number of advantages [2].

## 2 Approximation of wavelets for linear systems

A continuous-time wavelet transform is the L<sub>2</sub>-inner product of a wavelet  $\psi(t)$  with a signal  $f(t)$ . This type of transform can be implemented with an LS since if a time signal  $f(t)$  is passed through an LS, then  $f(t)$  is convoluted with the impulse response  $h(t)$  of that LS. As a result a wavelet transform can be approximated by an LS of finite order by approximating the time-reversed wavelet function  $\tilde{\psi}(t)$  with the impulse response  $h(t)$  of the LS. Only the implementation of (strictly) proper rational functions is feasible and therefore the wavelet should be shifted in time to avoid truncation of energy such that a time-reversed and shifted wavelet  $\tilde{\psi}(t)$  is approximated with impulse response  $h(t)$ .

## 3 L<sub>2</sub>-approximation of wavelets

L<sub>2</sub>-approximation theory provides a framework for studying the problem of wavelet approximation, which offers a number of advantages: firstly, it is quite appropriate to use the L<sub>2</sub>-norm to measure the quality of an approximation  $h(t)$  of the function  $\tilde{\psi}(t)$  since  $W(t, \sigma)$  is an L<sub>2</sub>-inner product. Secondly, it is desirable that the approximation  $h(t)$  of  $\tilde{\psi}(t)$  behaves equally well for all time instances  $t$ . As a third advantage L<sub>2</sub>-approximation allows for a description in the time domain as well as in the Laplace domain.

For the generic situation of stable systems with distinct poles, the impulse response function  $h(t)$  is a linear combination of damped exponentials and exponentially damped harmonics. This makes it possible for low order systems, to propose an explicitly parameterized class of impulse response functions among which to search for a good approximation of  $\tilde{\psi}(t)$ , as discussed in [3].

## 4 Obtaining a good starting point

In order to approximate a wavelet function with the L<sub>2</sub>-approach a starting point is required. The choice of this point is significant due to the existence of local optima. To obtain a good starting point for the L<sub>2</sub>-approximation approach, one can start by constructing a high-order model and applying model reduction with for example the balance and truncate method, so that an initial model with the appropriate order  $n$  is obtained. To do that we start with a sampled version of the time-reversed and shifted wavelet  $\tilde{\psi}(t)$ , from which a discrete-time MA-model is created, that is reduced, converted to continuous time and is further reduced such that it has the required order  $n$  as described in [4].

## References

- [1] S.A.P. Haddad, N. Verwaal, R. Houben and W.A. Serdijn, "Optimized dynamic translinear implementation of the Gaussian wavelet transform", *Proc. IEEE Int. Symposium on Circuits and Systems I*, 2004, pp 145–148.
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- [3] J.M.H. Karel, R.L.M. Peeters, R.L. Westra, S.A.P. Haddad and W.A. Serdijn, "Wavelet Approximation for Implementation in Dynamic Translinear Circuits", *Submitted, 16th IFAC World Congress*, 2005.
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