# An Ultra Low Power CMOS pA/V Transconductor and its Application to Wavelet Filters

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### ABSTRACT

Two topologies of ultra low-power CMOS triode transconductor are proposed. Its input transistors are kept in the triode region to benefit from the lowest  $g_m/I_D$  ratio. The  $g_m$  is adjusted by a well defined (W/L) and  $V_{DS}$ , the latter a replica of the tuning voltage  $V_{TUNE}$ . Transconductance down to hundreds of pA/V are obtained and used to implement a 6th order wavelet filter. The resulting design complies with a 1.5V supply and a 0.35µm CMOS process. The total power consumption of the wavelet filters using the first and second topology of transconductor equals 51nW and 114nW, respectively.

## **Categories and Subject Descriptors**

B.7.1 [Integrated Circuits]: Types and Design Styles - Advanced technologies, VLSI (very large scale integration).

#### **General Terms**

Performance, Design, Standardization.

#### Keywords

Low-power, pa/V, transconductor.

#### **1. INTRODUCTION**

In the field of medical electronics, active filters with large time constants are often required to design low cutoff-frequency filters (in the Hz and sub-Hz range), demanding the use of large capacitors or very low transconductance. To limit capacitors to practicable values, a transconductor with an extremely small transconductance  $g_m$  is needed.

This paper presents two topologies of ultra low-power transconductor. Both configurations are compact and have their input transistors operating in the triode region to benefit from the lowest  $g_m/I_D$  ratio and linear variation of  $g_m$ , which is controlled by an external voltage  $V_{TUNE}$ . The advantages of this technique with respect to the techniques that employ voltage attenuation, source degeneration or current splitting [2-5] can be found in [1]. The first  $g_m$ , named VLPT- $g_m$  (very low-power triode  $g_m$ ), with transconductance in the range of few nA/V. The second configuration, named Delta- $g_m$ , is presented here and the  $g_m$  can be adjusted to values down to hundreds of pA/V.

Subsequently, this paper presents an implementation of the wavelet transform with a Gaussian wavelet (*gaus1*) in an ultra low-power environment, using the proposed transconductors. Low-power analog realization of the continuous wavelet transform enables its application *in vivo*, e.g. in pacemakers and IECG recorders.

Previous work on analog realization of the continuous wavelet transform uses the dynamic-translinear circuit technique [6]. Contrary to this approach, the  $g_m$  is now controlled by voltage rather than by current. Translinear circuits become difficult to integrate when designing low cutoff-frequency filters for use in the Hz and sub-Hz range. As an example, for  $g_m = 1nA/V$ , the VLPT- $g_m$  needs to be biased with a quiescent current around  $I_Q = 300pA$ . To achieve the same time constant and considering the same bias current, the translinear circuit needs an increase of 12.6 times in capacitor value. Or, to maintain the same capacitor, it is necessary to decrease the current to 25pA, which is difficult to obtain precisely.

Since (W/L) offers a degree of freedom in sizing  $g_m$ ,  $V_{DS}$  values well above the equivalent noise of the biasing circuit can be set, while still obtaining a very-low  $g_m$ . Consequently, filters with more predictable frequency characteristics can be implemented. Owing to its extended linearity, the triode-MOSFET transconductor also handles larger signals, with no need for linearization techniques.

The paper organization is as follows. Section 2 introduces the triode transconductors circuits. Design procedures for realizing appropriate  $g_m$  values and implementing the wavelet filter are discussed in Section 3. Simulation results are used to demonstrate circuit performance and tunability in Section 4. Conclusions and final remarks are given in Section 5.

#### 2. TRANSCONDUCTORS DESCRIPTION

The proposed triode transconductors are shown in Fig. 1. Fig.1a shows the VLPT-gm, that is an improvement of the circuit introduced in [1]. The main difference of these circuits is the introduction of a common-gate stage  $M_{3A}$ - $M_{3B}$  into the loop of the auxiliary amplifier. The transconductor equivalent noise and output swing remain practically the same. However there is a great improvement in the auxiliary amplifier loop gain and transconductor output resistance  $R_{OUT}$ , as shown in Fig. 2.

Here,  $A_{L1}$  and  $A_{L2}$  represent the loop gain of the auxiliary amplifier in the original circuit in [1] and in the proposed transconductor, respectively, and are given by

$$A_{L1} \cong g_{m2}r_{ds2}, A_{L2} \cong g_{m2}r_{ds2}g_{m3}r_{ds3}$$
(1)

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Fig. 1. Triode Transconductors a)VLPT-gm and b) Delta-gm

Input transistors  $M_{1A}$ - $M_{1B}$  have their drain voltages regulated by an auxiliary amplifier that comprises  $M_{2A}$ - $M_{2B}$ ,  $M_{3A}$ - $M_{3B}$ ,  $M_{4A}$ - $M_{4B}$  and bias current sources  $M_{7A}$ - $M_{7B}$  and  $M_{8A}$ - $M_{8B}$ . Internal voltages  $V_B$ ,  $V_C$  and  $V_{DC}$  are derived from the bias circuit shown in Fig.3.

The bias generator is structurally alike the transconductor so that the external voltage  $V_{TUNE}$  is reflected to the drain of  $M_{1A}$ - $M_{1B}$ . A low voltage cascade current mirror comprising  $M_{5A}$ - $M_{5B}$  and  $M_{6A}$ - $M_{6B}$  provides a single-ended output.

Even though a common-drain configuration  $M_4$  is seen from the output node, the transconductor still exhibits a high output resistance, as the loop gain around  $M_2$ ,  $M_3$  and  $M_4$  is very large. Current sources  $M_7$  and  $M_8$  biased in their weak inversion region provide an output resistance, seen from the drain terminal of  $M_8$ ,  $R_8$ , in the order of  $10^{11}\Omega$ , so that an output resistance  $R_{OUT}$  of the same order is obtained.

The gate-voltage of  $M_{2A}$ - $M_{2B}$  is set to  $V_C = V_{TUNE} - V_{GS2}$ , whereas  $V_B$  imposes a bias current  $I_B$  through  $M_{7A}$ - $M_{7B}$ . Both voltages  $V_B$  and  $V_C$  are on-chip generated. Referring  $V_{TUNE}$  to  $V_{DD}$  and denoting  $\beta_1 = (W/L) 1 \mu_p C_{ox}$ , the transconductance of the entire circuit is

$$g_m = g_{m1} = \beta_1 V_{\text{TUNE}}$$
(2)

A second transconductor Delta-gm is shown in Fig.1b. The aspect-ratios of input transistors  $(M_{1A}-M_{1D})$  are  $(W/L)_{A,B} = (1 + \Delta)(W/L)_{C,D}$ .

Considering a balanced small signal voltage applied in  $V_{in\mathchar`+}$  and  $V_{in\mathchar`+}$  the output current is given by

$$i_{OUT} = (i_{1B} + i_{1D}) - (i_{1A} + i_{1C})$$

$$i_{OUT} = \frac{v_{IN}}{2} g_{m1D} \Delta + \frac{v_{IN}}{2} g_{m1C}$$

$$\therefore i_{OUT} = \Delta g_{m1C,D} v_{IN}$$
(3)

Referring  $V_{TUNE}$  to  $V_{DD}$  and denoting  $\beta$ =(W/L) $\mu_pC_{ox}$ , the overall transconductance is

$$g_m = \Delta g_{m1C,D} = \Delta \beta_{1C,D} V_{TUNE} \tag{4}$$



Fig. 2. Transconductor introduced in [1] and proposed transconductor output resistance as function of R<sub>8</sub>





(b) Fig. 3. Bias generator [1]: (a) circuit diagram and (b) the corresponding symbol

#### **3. WAVELET FILTER DESIGN**

#### 3.A. $L_2$ approximation

As mentioned in [6], approximation methods should be applied to obtain the required transfer function of a wavelet filter's impulse response. A method which proves to be successful is provided by Padé approximation of the Laplace transform of the impulse response h(t) of the filter [6]. Another alternative to find a suitable wavelet base approximation can be provided by the theory of L<sub>2</sub> approximation [7].

The advantage of the  $L_2$  method compared to the Padé approximation is that the  $L_2$  approximation offers a more global approximation, i.e., not concentrating on one particular point ---Padé is usually computed at the origin. Also, the fit is performed directly in the time domain yielding good control and easy interpretation of the optimization criteria. The  $L_2$  approximation technique is based on minimizing the least-mean-square-error. In this scheme the error integral, which is the difference between the wavelet function  $\psi(t)$  and its approximation h(t), is defined by

$$\varepsilon_{L2} = \int_0^\infty \left( \psi(t) - h(t) \right)^2 dt \tag{5}$$

In this  $L_2$  approach we first express the impulse response (in time domain) of a general filter. After that, the error  $\varepsilon_{L2}$  is minimized with respect to the poles and zeros of the wavelet filter. For the generic situation of stable systems with distinct poles, h(t) may typically have the following form [7]

$$h(t) = \sum_{i=1}^{n} A_{i} e^{p_{it}} = \sum_{i=1}^{k} c_{i} e^{p_{it}} + c_{k+1} e^{p_{k+1}t} \sin(p_{k+2}t) + c_{k+2} e^{p_{k+1}t} \cos(p_{k+2}t) + \cdots + c_{n-1} e^{p_{n-1}t} \sin(p_{n}t) + c_{n} e^{p_{n-1}t} \cos(p_{n}t)$$
(6)

where  $A_i$  and  $P_i$  can be real or complex numbers;  $c_i$  and  $p_i$  are real numbers, representing the impulse response function h(t) as a linear combination of damped exponentials and exponentially damped harmonics. *k* corresponds to the number of real poles and *n* is the order of the filter.

Then, given the explicit form of a wavelet base  $\psi(t)$  and the approximated impulse response h(t), the L<sub>2</sub>-norm of the difference  $\psi(t)$ -h(t) can now minimized in a straightforward way using standard numerical optimization techniques and software. The most direct way to find the minimum of Eq.5 is by computation of all partial derivatives of  $\varepsilon_{L2}$  with respect to A<sub>i</sub> and P<sub>i</sub> and setting them equal to zero, namely

$$\frac{\partial \varepsilon_{L2}}{\partial A_i}, \frac{\partial \varepsilon_{L2}}{\partial P_i} = 0 \qquad for \qquad i = 1 \dots n \tag{7}$$

The wavelet base approximation using the proposed  $L_2$  approach is given in Fig.4, where the first derivative of a Gaussian wavelet base (*gaus1*) has been approximated using the corresponding 6<sup>th</sup>order transfer function

$$H(s) = \frac{0.16s^4 - 8.32s^3 + 6.64s^2 - 139s}{s^6 + 5.9s^5 + 30.5s^4 + 83.1s^3 + 163s^2 + 176s + 93.3}$$
(8)



Fig. 4. L<sub>2</sub> approximation of the first derivative of Gaussian

#### 3.B. State-space filter implementation

To meet low-power low-voltage requirements, the state-space description of the filter has been optimized with respect to dynamic range, sparsity and sensitivity [6]. The filter design that follows is based on an orthonormal ladder structure and employs the nano-power g<sub>m</sub> transconductor described in the previous section as the basic building block of the filter diagram in Fig.5. In order to obtain the corresponding gm-C filter realization, we need first to map the state-space coefficients on the respective g<sub>m</sub> values. From Eq.2 of the transconductance, one can notice that we may vary the value of  $g_m$  by changing  $\beta_1$  (the aspect ration W/L) or the drain-source voltage  $(V_{TUNE})$  of transistor M1. However, due to the additional bias stages required to obtain different filter coefficients, realization of the various  $V_{TUNE}$  bias generators would increase the power consumption by a factor of  $(n-1) \cdot P_{Bias}$ , where n is the number of implemented coefficients and  $P_{Bias}$ represents the power consumption of the biasing stage. We thus opt for changing  $g_m$  by changing  $\beta_1$ .

#### **4. SIMULATION RESULTS**

To validate the circuit principle, we have simulated the wavelet Gm-C filter using models of AMS's  $0.35\mu m$  CMOS IC technology. The circuit has been designed to operate from a 1.5-V supply voltage. In order to implement the different coefficients of the state-space representation we can vary the width of input transistors  $M_1$  or the value of  $V_{TUNE}$ .

Fig. 5 shows the block diagram of the wavelet filter and the value of each  $g_m$ , which were reached by varying the width of input transistors @V<sub>TUNE</sub>=20mV. In Fig.6 one can see  $g_m$  ranging from 1nA/V to 5nA/V by changing V<sub>TUNE</sub> from 10mV to 50mV.

Finally, to implement a Wavelet Transform, we need to be able to scale and shift in time (and, consequently in frequency) the *gaus1* function. By changing the values of the  $V_{TUNE}$  accordingly we implement different scales, while preserving the impulse response waveform, as one can see in Fig.7.

Fig.8b illustrates 4 dyadic scales with center frequencies ranging from 14Hz to 120Hz for  $V_{TUNE}$  varying from 10mV to 80mV, respectively

Fig.9 shows the total harmonic distortion (THD) of VLPT- $g_m$  and Delta- $g_m$  with respect do  $V_{TUNE}$ . One can see a distortion THD < - 46dB for the range10mV <  $V_{TUNE}$  < 80mV.



Fig. 5. Block diagram of the wavelet filter



Fig. 6. Different  $g_m$  values obtained by varying  $V_{TUNE}$ 



Fig. 7 Impulse response filter scaling by changing  $V_{\text{TUNE}}$ 



Fig. 8 Frequency response filter scaling by changing  $V_{\text{TUNE}}$ 



Fig. 9. THD values obtained by varying  $V_{\text{TUNE}}$ 

Monte Carlo analysis for a spread of 5% on both (W/L) and  $V_{T0}$  parameters on input transistors of the  $g_m$  revealed a maximum variation of 2.6% in the transconductance value of VLPT- $g_m$ . Fig. 10 shows, for the same Monte Carlo analysis, the  $g_m$  variation of Delta- $g_m$  by changing the value of Delta.

A transconductor with Delta = 0.4 was set to implement the wavelet filter. One can thus see the trade-off between the value of  $g_m$  and precision of the transconductance.



Fig. 10. g<sub>m</sub> variation in Monte Carlo analysis by changing delta

Table 1 shows the summary of the simulated results. The total power consumption of Delta-g<sub>m</sub> filter equals 114nW, a factor of two compared with Delta-g<sub>m</sub>. Input-referred noise is  $156\mu V/\sqrt{Hz}$  @1Hz and  $119\mu V/\sqrt{Hz}$  @100Hz for VLPT-g<sub>m</sub>. Output resistance and distortion have similar results for both topologies. The great advantage of Delta-g<sub>m</sub> is its minimum value of transconductance and greater bandwidth. For example, with delta = 0.15 (g<sub>m</sub> variation around 5%), a minimum transconductance of 150pA/V is achieved. And for Delta = 0.4 the 3dB frequency of 1nA/V is 1.33 kHz and 24 kHz for VLPT-gm and Delta-gm, respectively. Such an improvement in the frequency response is due to the reduction of the dimension of transistors in the implementation of Delta-g<sub>m</sub>.

Table 1 – Summary of simulated results

	VLPT-gm	Delta-gm
Filter Power [nW]	51n	114
g <sub>m</sub> Band-width [kHz], delta=0.4	1.33	24
Input Eq. Noise @ 1Hz	156	642
Input Eq. Noise @ 100Hz	119	460
Minimum g <sub>m</sub> [nA/V]	≅ 1	≅ 0.15
Rout $@g_m = 2nA/V [\Omega]$	$1 \ge 10^{11}$	$4 \ge 10^{10}$
gm variation[%], $delta = 0.4$	2.7	2.9
$g_m$ variation[%], delta = 0.15	2.7	5
THD[dB], $V_{TUNE} = 20mV$	-53	-51
THD[dB], $V_{TUNE} = 80 \text{mV}$	-47	-53

#### **5. CONCLUSION**

Two compact CMOS transconductors suitable for ultra-low power gm-C filters operating in the Hz and sub-Hz range have been proposed. Its input transistors are kept in the triode-region to benefit from the lowest  $g_m/I_D$  ratio. To validate the circuit principle, the transconductors were used to implement a wavelet transform with a Gaussian wavelet using a 6th order  $L_2$  approximation.

The design was realized in accordance with VDD=1.5V and a 0.35 $\mu$ m n-well CMOS process. Simulation data were obtained with PSPICE and Bsim3v3 models. For the VLPT-g<sub>m</sub>, the transconductance ranges from 1nA/V to 12nA/V, total power consumption equals 51nW, for a total capacitance of 120pF. For Delta-gm filter, g<sub>m</sub> spans from 400pA/V to 4.8nA/V, with total power consumption of 114nW, for a total capacitance of 48pF. THD < 1% @200mVpeak\_value was reached for every transconductor of the filters.

The simulated step response of 6th order wavelet filter differs only slightly from the approximated response in both topologies. From this, we can conclude that the coefficients have been implemented successfully.

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